"Measurement of the t t-bar Production Cross Section in pp Collisions at 7 TeV in Lepton + Jets Events Using b-quark Jet Identification"

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ABSTRACT

A new measurement of the inclusive production cross section for pp to t t-bar is performed at a center-of-mass energy of 7 TeV using data collected by the CMS experiment at the LHC. The analysis uses a data sample corresponding to an integrated luminosity of 36 inverse picobarns, and is based on the final state with one isolated, high transverse momentum muon or electron, missing transverse energy, and hadronic jets. The t t-bar content of the selected events is enhanced by requiring the presence of at least one jet consistent with b-quark hadronization. The measured cross section is 150 ±/− 9 (stat.) +/− 17 syst.) +/− 6 (lumi.) pb and is in agreement with higher-order QCD calculations. The combination of this measurement with a previous CMS result based on dileptons gives 154 ±/− 17 (stat.+syst.) +/− 6 (lumi.) pb.

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Measurement of the $t\bar{t}$ production cross section in $pp$ collisions at 7 TeV in lepton + jets events using $b$-quark jet identification

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A new measurement of the inclusive production cross section for $pp \rightarrow t\bar{t}$ is performed at a center-of-mass energy of 7 TeV using data collected by the CMS experiment at the LHC. The analysis uses a data sample corresponding to an integrated luminosity of 36 pb$^{-1}$, and is based on the final state with one isolated, high transverse momentum muon or electron, missing transverse energy, and hadronic jets. The $t\bar{t}$ content of the selected events is enhanced by requiring the presence of at least one jet consistent with $b$-quark hadronization. The measured cross section is $150 \pm 9$(stat) $\pm 17$(syst) $\pm 6$(lumi) pb and is in agreement with higher-order QCD calculations. The combination of this measurement with a previous CMS result based on dileptons gives $154 \pm 17$(stat + syst) $\pm 6$(lumi) pb.

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I. INTRODUCTION

The top quark was first observed in proton-antiproton collisions at $\sqrt{s} = 1.8$ TeV at the Fermilab Tevatron collider [1,2]. Since then its properties have been studied by the Tevatron experiments and found to be in agreement with the expectations of the standard model [3]. At the Large Hadron Collider (LHC) [4] top-quark production can be studied in $pp$ collisions at $\sqrt{s} = 7$ TeV, allowing extended measurements of the top quark properties. A precise measurement of these properties is important as top-quark production may be a background for new physics.

At the LHC top quarks can be produced singly or in pairs. This paper focuses on the study of the $t\bar{t}$ final state, for which the production cross section has been calculated in next-to-leading-order (NLO) and approximate next-to-next-to-leading-order (NNLO) quantum chromodynamics (QCD) [5–7]. In the standard model the top quark decays almost 100% of the time via the weak process $t \rightarrow Wb$. We focus on the $t\bar{t}$ decays in which one of the two $W$ bosons decays hadronically and the other decays leptonically (the semileptonic channel), giving a final state containing an electron or muon, a neutrino, and four jets, two of which come from the hadronization of $b$ quarks. Here taus are detected only through their semileptonic decays to electrons and muons. The results are based on the analysis of a data sample corresponding to an integrated luminosity of 36 pb$^{-1}$ [8], which was recorded by the Compact Muon Solenoid (CMS) experiment between April and November 2010.

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allowing for energy balance measurements in the plane transverse to the beam direction. A two-tier trigger system selects the most interesting $pp$ collision events for use in physics analysis. A more detailed description of the CMS detector can be found elsewhere [12].

We describe the data and event selection in Sec. II of this paper, followed by a brief description of the modeling of the signal and background processes in Sec. III. Sec. IV describes the method used to extract the cross section from the selected events, as well as the calculation of the statistical and systematic uncertainties on the result. The cross-check analyses are discussed briefly in Sec. V. Lastly, in Secs. VI and VII we present a summary of all of the CMS measurements and compare the results with the predictions from QCD.

II. EVENT SELECTION

The trigger used to select the data samples for analysis is based on the presence of at least one charged lepton, with either an electron or a muon with a transverse momentum, $p_T > p_{\text{min}}^T$. Because of increasing maximum instantaneous luminosity, the minimum transverse momentum was varied between 9 and 15 GeV for muons and between 10 and 22 GeV for electrons in order to maintain a reasonable trigger rate. The same data are used both for signal selection and for the study of the nonstop QCD multijet and $W(Z) +$ jets backgrounds. The data sets corresponding to the various triggers can be treated together, as the transverse momentum thresholds used for the offline analysis are significantly higher. The triggers have been shown to have efficiencies of $92.2 \pm 0.2\%$ and $98.2 \pm 0.1\%$ for the muon and electron channels, respectively, based on independent studies of $Z$ boson decays into $\mu^+\mu^-$ and $e^+e^-$ pairs. No azimuthal nor polar angle dependence is observed.

Muons are reconstructed using the information from the muon chambers and the silicon tracker and required to be consistent with the reconstructed primary vertex [13]. A kinematic selection requiring $p_T > 20$ GeV and $|\eta| < 2.1$ is then used to select muon tracks for further analysis. Electrons are reconstructed using a combination of shower shape information and track/electromagnetic-cluster matching [14]. A veto is applied to reject the electrons coming from photon conversions. To be retained for further analysis, electron candidates are required to have a transverse energy, $E_T > 30$ GeV and $|\eta| < 2.5$, excluding the transition region between the barrel and end cap calorimeters, $1.44 < |\eta_e| < 1.57$, where $\eta_e$ is the pseudorapidity of the electromagnetic-cluster.

Signal events are required to have only one isolated lepton, whose origin is consistent with the reconstructed $pp$ interaction vertex [15]. Since the muon (electron) from a leptonic $W$ decay is expected to be isolated from other high-$p_T$ particles in the event, its track is required to be isolated from other activity in the event. This is done by requiring a relative isolation ($I_{\text{rel}}$) less than 0.05 for muons and 0.10 for electrons. A looser cut is used in the electron case to allow for the increased amount of radiation close to the track. Relative isolation is defined as $I_{\text{rel}} = (I_{\text{charged}} + I_{\text{neutral}} + I_{\text{photon}})/p_T$, where $p_T$ is the transverse momentum of the lepton, and $I_{\text{charged}}$, $I_{\text{neutral}}$, and $I_{\text{photon}}$ are the sums of the transverse energies of the charged and neutral hadrons and the photons reconstructed in a cone of $\Delta R < 0.3$ around the lepton direction, where $\Delta R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2}$. The energy deposited by the lepton is explicitly removed from the sums by defining an exclusion cone of $\Delta R < 0.15$ around the lepton direction. From studies based on $Z$ decays in the data, the combined identification and isolation efficiencies for these selections are $83 \pm 1\%$ for muons and $75 \pm 1\%$ for electrons.

Semileptonic $t\bar{t}$ events have at least four hadronic jets (from the hadronization of the bottom and light quarks). Charged and neutral hadrons, photons, and leptons are reconstructed using the CMS particle-flow algorithm [16] before they are clustered to form jets using the anti-$k_T$ jet algorithm [17] with a cone size $\Delta R = 0.5$. The jet clustering software used is FASTJET version 2.4.2 [18,19]. At least one jet candidate with $p_T > 25$ GeV and $|\eta| < 2.4$ is required, which must not overlap with a muon or electron candidate within $\Delta R < 0.3$. Relative and absolute jet energy corrections [20] are applied to the raw jet momenta to establish a uniform jet response in $p_T$ and $\eta$ (with uncertainties of $3–6\%$, dependent on $p_T$ and $\eta$). An offset correction, determined from simulation, is made to correct for the effects of event pileup (with an uncertainty <1.4%). There is an additional $b$-jet energy scale uncertainty which accounts for the differences in response between PYTHIA and HERWIG simulations ($\sim 3\%$). Lastly, a further 1.5% uncertainty is added to allow for residual calibration differences during different run periods for a total of 4.7–7.0%.

The neutrino from the leptonic $W$ decay escapes detection. Its presence is inferred from a sizeable transverse energy imbalance in the detector. The missing transverse energy ($E_T$) is defined as the negative of the vector sum of the transverse energies ($E_T$) of all of the particles found by the particle-flow algorithm. This is used as an event selection variable in both the muon and electron analyses to suppress the background from QCD multijet events, and is required to be greater than 20 GeV in both channels.

Because of the combined effects of the long $b$-quark lifetime ($\sim 1.5$ ps) and the fact that the $b$ quarks are produced with a significant boost, the decays of $b$-flavored hadrons are quite different from the shorter lived hadronic states. Rather than having an origin consistent with the primary collision vertex, they can travel a measurable distance before decaying, resulting in a displaced decay vertex. The origin of the particles from the $b$ decay is thus typically inconsistent with the primary vertex position. In the case of a semileptonic $b$-hadron decay, this
results in the production of a lepton with a displaced origin, that is also embedded inside a jet. These characteristics can be used to identify $b$-quark jets and distinguish them from their non-$b$ counterparts. Here we use a displaced secondary vertex algorithm to tag $b$ decays and suppress the background from $W(Z)$ + jet and QCD multijet events. The algorithm is described in detail in [21] and has a $b$-tag efficiency of 55% with a light parton ($u, d, s, g$) mistag rate of 1.5% for jets with $p_T > 30$ GeV in simulated QCD events. The event selection requires that at least one of the selected jets is $b$ tagged.

### III. SIGNAL AND BACKGROUND MODELING

The efficiency for selecting lepton + jets signal events and the corresponding kinematic distributions are modeled using a simulated $t\bar{t}$ event sample. The simulation is performed using MADGRAPH [22], where the events containing top-quark pairs are generated accompanied by up to three extra partons in the matrix-element calculation. The parton configurations generated by MADGRAPH are processed with PYTHIA 6.4[23] to provide fragmentation of the generated partons. The shower matching is done using the Kt-MLM prescription [22]. The generated events are then passed through the full CMS detector simulation based on GEANT4 [24].

The production of $W(Z) +$ jets events, where the vector boson decays leptonically, has a similar signature and constitutes the main background. These are also simulated using MADGRAPH. We use a dynamical mass scale ($Q^2$ scale) of $(m_W/Z)^2 + (\sum p_T^2)^2$ for the renormalization and factorization scales for both the $W +$ jets and $Z +$ jets simulations, and these scales are varied by factors of 2.0 and 0.5 in systematic studies.

In addition to the Monte Carlo generation using MADGRAPH, QCD multijet samples were produced using PYTHIA.

The QCD predictions for the top-quark pair production cross section are $157^{+32}_{-23}$ pb in NLO [25] and $164^{+10}_{-13}$ pb [5,6] or $163^{+11}_{-10}$ pb [7] in approximate NNLO. In each case the quoted uncertainties include the renormalization and factorization scale uncertainties, the uncertainties from the choice of parton distribution functions (PDF)s, and the uncertainty of the strong coupling constant ($\alpha_s$). For the scale uncertainty we have varied the renormalization and factorization scales by factors of 2 and 0.5 around the central choice of $(2m_t)^2 + (\sum p_T^2)^2$ with $m_t = 172.5$ GeV. The PDF and $\alpha_s$ uncertainties were determined by following the results obtained by using the MSTW2008 [26], CTEQ6.6 [27], and NNPDF2.0 [28] sets and combining the results using the PDF4LHC prescriptions [29].

Single-top-quark production is described in terms of the cross sections in the $s, t$ and $tW$ channels. The largest cross section is in the $t$ channel where the predicted NLO cross section is $\sigma_t = 64.6^{+3.4}_{-3.3}$ pb from MCFM [25,30–32]. The result is given for a scale of $(m_t)^2 + (\sum p_T^2)^2$ and an uncertainty that is defined in the same way as for top-quark pair production. Similarly, the cross sections for the $tW$ and $s$ channels are predicted to be $\sigma_{tW} = 10.6 \pm 0.8$ pb and $\sigma_s = 4.2 \pm 0.2$ pb [30], respectively. A measurement of the $t$-channel cross section has been performed by CMS and is found to be consistent with the value predicted by the standard model [33].

The inclusive NNLO cross section of the production of $W$ bosons decaying into leptons has been determined as $\sigma_{W\rightarrow l\nu} = 31.3 \pm 1.6$ nb using FEWZ [34] (corresponding to a $k$-factor of 1.3), setting renormalization and factorization scales to $m_W^2$ with $m_W = 80.398$ GeV. The uncertainty was determined in a similar way as for top-quark pair production. Finally, the Drell-Yan production cross section at NNLO has been calculated using FEWZ as $\sigma_{Z/\gamma\rightarrow l\bar{l}}(m_{ll} > 50$ GeV) = $3.0 \pm 0.1$ nb where the scales were set to $m_Z^2$ with $m_Z = 91.1876$ GeV.

The cross sections discussed above are used to normalize the simulated event samples. The profile likelihood fit yields corrections to these values. The normalizations for the final comparisons with the data are determined from fits to the data in control samples.

### IV. CROSS SECTION MEASUREMENTS

The following subsections discuss the measurement procedure and the results obtained from the analysis of the muon, electron and combined channels.

#### A. Fit procedure

To extract the $t\bar{t}$ cross section we perform a maximum likelihood fit to the number of reconstructed jets ($j = 1$–4, $\geq 5$), the number of $b$ tagged jets ($i = 1$, $\geq 2$), and the secondary vertex mass distribution in the data. The secondary vertex mass is defined as the mass of the sum of the four-vectors of the tracks associated to the secondary vertex, assuming that each particle has the pion mass. It gives a good discrimination between the contributions from light- and heavy-flavor quark production (Fig. 1). We fit the data to the sum of signal and background shapes using a binned Poisson likelihood.

The templates for the fit are normalized to the expected event yields for 36 pb$^{-1}$. The expected yield for each component in a given jet-multiplicity bin $j$ and tag-multiplicity bin $i$ is a function of the cross section, the jet energy scale (JES), the $b$-tag efficiency, and the background normalization. The JES and the $Q^2$-scales affect the jet-multiplicity, and the $b$-tag efficiency impacts the number of $b$ tags. The background model depends on each of these and has additional contributions from the normalization and extrapolation from the sidebands in the data. Because these effects are expected to cause the largest uncertainties on the $t\bar{t}$ cross section measurement, and
they are correlated, they are treated as nuisance parameters in the profile likelihood fit. The minimization of the likelihood thus provides simultaneous measurements of each contribution and the $t\bar{t}$ cross section.

We determine the background normalizations from data sideband regions and extrapolate to the signal region using various models. In particular, the four major backgrounds are $W$ + jets, $Z$ + jets, single-top-quark, and QCD multijet production.

The templates for the $W$ and $Z$ contributions are normalized such that the NNLO predictions are equal to unity. During the profile likelihood maximization, the normalizations of these components are extracted. A full detector unfolding is not done, so this is not a meaningful measurement of the $W(Z)$ + jets cross section, however the impact of the renormalization and factorization scales on the $t\bar{t}$ cross section is found to be smaller than that predicted by an ad hoc variation of the scales.

The $W$ and $Z$ + jets backgrounds come from $V + b$ jets, $V + c$ jets, and $V +$ light flavor events. The same $k$-factor of 1.30 (defined in Sec. III) is applied to all three flavors as inputs to the likelihood fit (although the three components are allowed to float independently in the fit). An additional electroweak background is single-top ($s$ and $t$ and $tW$ channels) events.

The shape of the jet-multiplicity distribution ($N_{\text{jet}}$) depends on the choice of the jet $p_T$ threshold, and thus is also sensitive to the jet energy scale (JES). In this sense, the fit is intrinsically able to determine the JES from the variations of the $N_{\text{jet}}$ distribution as a function of JES. The uncertainty in the $b$-tag efficiency is also extracted directly from the fit, by using the changes in the relative rates of one-tag, and two-tag events. A larger $b$-tag efficiency will result in events moving from one-tag to two-tag samples. In contrast, an overall increase in all tag bins together would indicate an increase in the $t\bar{t}$ cross section. The combined in situ measurement of the yields of principal backgrounds and parameters describing main systematic uncertainties leads to a significant improvement over analyses which use more conventional techniques for tagged cross section measurements.

There are several “nonprompt-$W$” or “QCD” backgrounds for the muon and electron analyses. The QCD background for the muon-plus-electron channel comes from multijet events with heavy flavor decays, kaon and pion decays in flight, and hadronic punchthrough in the muon system. Because these are difficult to calculate to the required precision we derive these backgrounds from the data. The normalization is determined by using a comparison of data and simulation in the data sideband region with $E_T < 20$ GeV. The ratio is used to scale the predicted yields for $E_T > 20$ GeV. The shapes and normalizations of the $t\bar{t}$, $W$ and $Z$ + jets are well described by the Monte Carlo simulation and are modeled that way. The shape of the QCD component is derived from the nonisolated ($|E_{\text{rel}}| > 0.2$) data. Because of the correlations between $E_T$ and isolation, the templates for the QCD estimate from the data that are taken from nonisolated samples are modified using the shape taken from the QCD simulation. This treatment is similar in spirit to the QCD treatment in the recent CMS $W$ and $Z$ cross section measurements [35]. The QCD rate in each jet bin is constrained to the average of the true $E_T$ distribution of the nonisolated region, and the “modified” $E_T$ distribution after accounting for correlations from the Monte Carlo simulation. The QCD component in the fit is constrained to 100% of the rate or half the difference between the results, whichever is greater.

The secondary vertex mass shapes for the fit are taken from the nonisolated data. Because of limited statistics, the $\geq 3$ jet sample is included as a single template, with separate normalizations for each jet bin.

Similarly, the electron-plus-jets channel is contaminated by photon conversions, jets with a high electromagnetic fraction, and heavy flavor decays. The normalization of this background is also estimated from a fit to the $E_T$ spectrum. However, the nonisolated sidebands do not accurately represent the shape of the $E_T$ distribution, and so the shape is determined by reversing at least two out of six of the electron identification criteria. The ensemble of these “marginal failures” makes a good representation of the shape of the $E_T$ background for this background source. This shape is then fit with the same $E_T$ procedure as in the muon case.

There are alternative control samples for both the jet energy scale, and the $b$-tag efficiency. The jet energy scale is measured as described in Sec. II. The uncertainty measured there is used in a Gaussian constraint on the jet energy scale in the likelihood (approximately 4%). The $b$-tagging efficiency and light quark mistag rate have been measured in an independent sample of QCD dijet events [36], and these values are input as Gaussian constraints on the parameters in the likelihood. Specifically, the $b$-tag

FIG. 1 (color online). Secondary vertex mass distribution for bottom, charm, and light flavor jets. The bottom and charm templates are taken from simulated $t\bar{t}$ events and the light flavor shape is taken from simulated $W$ + jet events.
efficiency scale factor is constrained to $1.0 \pm 0.2$, and the mistag rate scale factor is constrained to $1.0 \pm 0.1$. The technical implementation of these efficiencies in the likelihood is to weight the tagged jets in the simulation up or down by the data-to-simulation scale factor, and weight untagged jets in the simulation with zero weight.

The number of predicted events with respect to each contribution is given by Eqns. (1)–(3), for the $t\bar{t}$ signal and two of the $W + b$-jets backgrounds ($W + b$-jets and $W + b$-jets background, and the single-top, and the QCD multijet production. Thus we have

$$N_{t\bar{t}}^{\text{pred}}(i, j) = K_{\bar{t}} \cdot N_{t\bar{t}}^{\text{MC}}(i, j) \cdot P_b^{\text{tag}}(i, j, R_b^{\text{tag}}) \cdot p^{\text{mistag}}(i, j, R^{\text{mistag}}) \cdot P^{\text{JES}}(i, j, R^{\text{JES}})$$

$$N_{Wbb}^{\text{pred}}(i, j) = K_{Wbb} \cdot N_{Wbb}^{\text{MC}}(i, j) \cdot P_b^{\text{tag}}(i, j, R_b^{\text{tag}}) \cdot p^{\text{mistag}}(i, j, R^{\text{mistag}}) \cdot P^{\text{JES}}(i, j, R^{\text{JES}})$$

$$N_{Wqq}^{\text{pred}}(i, j) = K_{Wqq} \cdot N_{Wqq}^{\text{MC}}(i, j) \cdot p^{\text{mistag}}(i, j, R^{\text{mistag}}) \cdot P^{\text{JES}}(i, j, R^{\text{JES}}) \cdot P^{Q^2}(i, j, R^{Q^2})$$

where $K_{\bar{t}}$ is the fitted scale factor for the NLO prediction for $t\bar{t}$; $i$ and $j$ run over tags and jets, respectively; $K_{Wbb}$ is the fitted scale factor for the NNLO prediction for $Wbb$ (etc.); $N_{t\bar{t}}^{\text{MC}}(i, j)$ is the number of events expected for sample $X$, derived from Monte Carlo and corrected with data-to-Monte-Carlo scale factors. The $P(i, j, X)$ factors are multiplicative functions accounting for the relative differences with respect to the input expected yield, as a function of the assumed value $R_X$ of nuisance parameter $X$ (i.e., $b$-tag efficiency, jet energy scale, etc.) These are interpolated from various configurations in the simulation with polynomials. The convention chosen is that the nominal event yield is at $R_X = 0$ (i.e., no variation in parameter $X$), and $P(i, j, X) = 1.0$ (i.e., multiplicative factor of 1.0 by default). The “+1σ” variation is at $R_X = 1$, and the “-1σ” variation is at $R_X = -1$.

The fit minimizes the negative log likelihood, summing over the histogram bins ($k$) of the secondary vertex mass, the number of jets ($j$), and the number of tags ($i$). The various constraints (described above) are included as Gaussian penalty terms on the variables, which are represented by $C_X$. The full profile likelihood expression is

$$-2 \ln L = -2 \left\{ \sum_{i,j} \sum_k \ln(P(N^{\text{obs}}_k(i, j)), N^{\text{exp}}_k(i, j)) \right\}$$

$$- \frac{1}{2} \sum_i \left\{ \frac{(C_X - \hat{C}_X)^2}{\sigma_{C_X}^2} \right\}$$

where $\mathcal{P}$ is a Poisson probability that the predicted yield ($N^{\text{exp}}_k$) given by the various components statistically overlaps with the data ($N^{\text{obs}}_k$) in each tag/jet bin $i$, $j$, given by

$$\ln \mathcal{P}(x, y) = x \ln y - y - \ln \Gamma(x + 1),$$

where $\Gamma(x)$ is the Gamma function.

Table I shows a summary of all of the inputs to the profile likelihood, along with the constraints.

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Constraint (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$b$-tag Efficiency scale factor</td>
<td>20</td>
</tr>
<tr>
<td>$b$-tag Mistag scale factor</td>
<td>10</td>
</tr>
<tr>
<td>Jet energy scale relative to nominal</td>
<td>4</td>
</tr>
<tr>
<td>$W + j$-jets renormalization/factorization scales</td>
<td>$\pm 100$</td>
</tr>
<tr>
<td>$W + j$-jets background normalization</td>
<td>unconstrained</td>
</tr>
<tr>
<td>QCD background normalization</td>
<td>100</td>
</tr>
<tr>
<td>Single-top background normalization</td>
<td>30</td>
</tr>
<tr>
<td>$Z + j$-jets background normalization</td>
<td>30</td>
</tr>
</tbody>
</table>

There are also a number of systematic uncertainties that are not included directly in the profile likelihood and hence are taken as additional systematic uncertainties outside of the fit result. The largest of these is the systematic uncertainty due to the overall luminosity determination. It has also been shown on independent samples of $Z \rightarrow ee$ and $Z \rightarrow \mu\mu$ events, that the efficiencies for triggering, reconstructing, and identifying isolated leptons of this type are very similar in the data and simulations. We have corrected for the small differences observed. The effect of these uncertainties are not included in the profile likelihood, and hence are taken as an additional systematic uncertainty of 3%.

In all of the cases that are described below, the robustness of the statistical procedure is demonstrated with
a priori pseudoexperiments where the expected yields and the parameters in the profile likelihood are sampled randomly according to Poisson or Gaussian statistics (as appropriate). In cases where the true frequentist statistical coverage is not achieved due to the limitations of the profile likelihood method, coverage is assured by correcting for the slight biases (of order 1–2% in the central values and/or uncertainties).

B. Muon + Jet analysis

For the muon channel we make two modifications to the basic event selection discussed above. Instead of using the isolation cut of $I_{\text{rel}} < 0.05$, we require that the selected muon tracks are found to be isolated by the particle-flow reconstruction and pass a cut of $I_{\text{rel}} < 0.15$. The results of the fit are shown in Table II. The fit considers events with one tag (1-tag) and two and more tags (2-tag) separately, giving nine jet-tag “bins” (subsamples) which are fit by the joint likelihood. Table II lists the observed and fitted rates for each jet-tag bin.

![Table II](image)

Table III lists the systematic uncertainties from the fit. These include both the theoretical uncertainties from the $t\bar{t}$ modeling and the corrections used to match the simulations to the data and give a total uncertainty of 4.3% for the $t\bar{t}$ signal model. The unclustered energy in the detector results in an additional resolution uncertainty of $<1\%$ on the $E_T$ scale. We combine these with the data-simulation uncertainties due to the jet energy scale and jet resolution modeling, the $b$-tag efficiency and mistag rate and obtain a total systematic uncertainty of 12.5%. For illustrative purposes, in Table III, we have broken up the pieces of the profile likelihood and quote the uncertainties due to the individual contributions. These are the result of fixing all of the other parameters of the likelihood and only allowing the chosen term to vary.

This yields a cross section measurement of

$$\sigma_{t\bar{t}} = 145 \pm 12\text{(stat)} \pm 18\text{(syst)} \pm 6\text{(lumi)} \text{ pb},$$

where the last uncertainty corresponds to the 4% uncertainty on the total integrated luminosity [8]. The fit
provides in situ measurements of the scale factors for both $b$ tagging and the jet energy scale. We obtain a result of $98 \pm 6\%$ for the $b$-tag scale factor and $92 \pm 9\%$ for the jet energy calibration. The scale factors for the $W + b$ jets and $W + c$ jets components indicate that the contributions in the data may be larger than what is expected by the predictions. For the $W + b$ jets component we find a cross section scale factor of $2.6^{+0.3}_{-0.2}$ and for the $W + c$ jets contribution we obtain $1.3^{+0.3}_{-0.2}$. It is also found that the $W +$ jets data are slightly harder than the central value of the renormalization and factorization scales chosen.

### C. Electron + Jets analysis

The analysis in the electron channel is performed in the same way as for the muon case. The results are shown in Table IV. The fit was performed in the same manner as for the muon channel, resulting in nine jet-tag bins (subsamples), which were fit by a joint likelihood, as described in

<table>
<thead>
<tr>
<th></th>
<th>Data</th>
<th>Fit</th>
<th>$\bar{t}t$</th>
<th>$t(\bar{t})$</th>
<th>$W + b$ jets</th>
<th>$W + c$ jets</th>
<th>$W + q\bar{q}$</th>
<th>$Z +$ jets</th>
<th>QCD</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 jet 1 $b$ tag</td>
<td>388</td>
<td>389.8</td>
<td>6.0</td>
<td>14.1</td>
<td>42.4</td>
<td>249.5</td>
<td>26.9</td>
<td>3.1</td>
<td>47.9</td>
</tr>
<tr>
<td>2 jets 1 $b$ tag</td>
<td>252</td>
<td>245.3</td>
<td>31.7</td>
<td>21.0</td>
<td>44.4</td>
<td>104.0</td>
<td>14.8</td>
<td>3.3</td>
<td>26.2</td>
</tr>
<tr>
<td>3 jets 1 $b$ tag</td>
<td>159</td>
<td>156.0</td>
<td>62.7</td>
<td>12.2</td>
<td>23.5</td>
<td>34.4</td>
<td>5.1</td>
<td>2.1</td>
<td>16.0</td>
</tr>
<tr>
<td>4 jets 1 $b$ tag</td>
<td>71</td>
<td>80.7</td>
<td>60.6</td>
<td>4.8</td>
<td>8.2</td>
<td>9.2</td>
<td>1.4</td>
<td>0.8</td>
<td>-4.3</td>
</tr>
<tr>
<td>$\geq 5$ jets 1 $b$ tag</td>
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<td>52.1</td>
<td>40.9</td>
<td>1.6</td>
<td>2.6</td>
<td>3.0</td>
<td>0.5</td>
<td>0.4</td>
<td>3.0</td>
</tr>
<tr>
<td>2 jets $\geq 2$ $b$ tags</td>
<td>14</td>
<td>19.9</td>
<td>9.4</td>
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<td>4.7</td>
<td>1.2</td>
<td>0.1</td>
<td>0.2</td>
<td>2.0</td>
</tr>
<tr>
<td>3 jets $\geq 2$ $b$ tags</td>
<td>39</td>
<td>38.1</td>
<td>29.1</td>
<td>3.1</td>
<td>3.8</td>
<td>0.9</td>
<td>0.0</td>
<td>0.2</td>
<td>0.9</td>
</tr>
<tr>
<td>4 jets $\geq 2$ $b$ tags</td>
<td>37</td>
<td>41.3</td>
<td>37.1</td>
<td>1.9</td>
<td>1.9</td>
<td>0.4</td>
<td>0.0</td>
<td>0.1</td>
<td>0.0</td>
</tr>
<tr>
<td>$\geq 5$ jets $\geq 2$ $b$ tags</td>
<td>37</td>
<td>30.7</td>
<td>28.8</td>
<td>0.9</td>
<td>0.8</td>
<td>0.2</td>
<td>0.0</td>
<td>0.1</td>
<td>0.0</td>
</tr>
<tr>
<td>Total</td>
<td>1054</td>
<td>1053.8</td>
<td>306.3</td>
<td>61.8</td>
<td>132.1</td>
<td>402.7</td>
<td>48.9</td>
<td>10.3</td>
<td>91.6</td>
</tr>
</tbody>
</table>

![Figure 2](color online). Results of the combined muon and electron channel fit. The muon channel is shown on the left and the electron channel on the right. The plots on the top are for exactly 1 $b$ tag and those on the bottom are for $\geq 2$ $b$ tags. The histograms within the top panel correspond to events with 1, 2, 3, 4 and $\geq 5$ jets, respectively, while the bottom panel shows histograms corresponding to events with 2, 3, 4 and $\geq 5$ jets.
Sec. IV A. Table IV lists the observed and fitted rates for each jet-tag bin. Note that the fit parameters are unbounded to avoid problems with bias. This can result in negative values for the event counts, as in the case of the 4 jets 1 tag yield for QCD in Table IV.

The resulting cross section is

$$\sigma_{tt} = 158 \pm 14(\text{stat}) \pm 19(\text{syst}) \pm 6(\text{lumi}) \text{ pb} \quad (7)$$

From the fit we obtain a result of $97 \pm 6\%$ for the $b$-tag scale factor and $103 \pm 8\%$ for the jet energy calibration. The scale factors for the $W + b$ jets and $W + c$ jets components are $1.4^{+0.4 \pm 0.3}$, respectively. These are in agreement with the results from the muon channel. The contributions to the systematic uncertainty are summarized in Table III.

D. Simultaneous muon and electron channel analysis

Having established the consistency of the separate channel measurements, we now proceed to perform a combined fit to both channels. To establish our best measurement, we repeat the fit procedure and apply it simultaneously to the data in both the electron and muon channels. We find that the resulting fitted event yields in each tag category are in good agreement with those obtained from the separate

FIG. 3 (color online). Kinematic distributions of the total transverse energy ($H_T$), the missing transverse energy ($E_T^{\text{miss}}$) and the transverse mass of the $W$ ($M_T^W$). The plots are for $\geq 3$ jets and $\geq 1 b$ tag and the comparison histograms correspond to the fitted values. The muon channel is shown on the left and the electron channel is on the right.

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channel fits (Tables II and IV), Figure 2 shows the comparison of the corresponding observed and fitted vertex mass distributions. Figure 3 shows the data for ≥ 3 jets and ≥ 1 b tag, and the fit results for the total transverse energy of the event ($E_T^\text{miss}$), the missing transverse energy ($E_T^\text{miss}$), and the transverse mass of the $W (M_{T}^W)$. We find good agreement in all cases.

The correlation matrix for the combined fit is listed in Table V. All of the terms are as defined in the text. The combined analysis cross section measurement is

$$\sigma_{bb} = 150 \pm 9(\text{stat}) \pm 17(\text{syst}) \pm 6(\text{lumi}) \text{ pb,}$$

which is in good agreement with both the separate channel measurements and those from the cross-check analyses discussed below. The corresponding summary of the systematic uncertainties is given in Table III. We obtain a result of 96$^{+5}_{-4} \%$ for the b-tag scale factor which agrees well with the result obtained in [21]. For the jet energy scale we obtain a result of 107$\pm 6\%$ indicating that the data may prefer a small increase in the jet energy calibration. The scale factors for the $W + b$ jets and $W + c$ jets components indicate that the contributions to the data may be larger than what is predicted by the scaled NNLO predictions of 110 pb and 3.0 nb. For the $W + b$ jets contribution we find a cross section scale factor of 1.9$^{+0.8}_{-0.5}$, which is similar to recent observations at the Tevatron [37–39]. The result for the $W + c$ jets contribution is 1.4$\pm 0.2$.

### V. CROSS-CHECK ANALYSES

As a cross-check of our results, we have performed a series of independent analyses in both the muon and electron channels. A summary of these is given in the following subsections. These use not only different analysis techniques but also different methods to suppress the backgrounds from $W + j$ and QCD multijet events. Each analysis requires at least three jets with $p_T > 25$ GeV and has no requirement on the amount of missing transverse energy. In addition, two different tagging algorithms are used for the two analyses in the muon channel. The neural network analysis uses a track-counting algorithm which counts the number of tracks nonassociable to the primary vertex [21] and the second analysis uses the muons from semileptonic b decays to tag b jets. Each analysis has significantly different systematic uncertainties from the analysis presented above and thus provides a good test of the robustness of the measurements. While there are some differences in the selected event samples, we do not attempt to combine the results because of the substantial overlap.

#### A. Neural network analysis with a track-counting b-tagger

The first cross-check is performed in the muon channel. It makes use of a multilayer perceptron neural network to distinguish $t\bar{t}$ signal events from the backgrounds after requiring a muon and three jets to pass the selection criteria. The network discriminant is built from the analysis of three input variables: the pseudorapidity $|\eta|$ of the muon, the distance $\Delta R_{12}$ in $\eta$-$\phi$ space between the two highest-$p_T$ jets in the event, and a boolean variable indicating the presence of at least one $b$ tagged jet. The network was trained using simulated samples of signal and background events and the cross section was determined by fitting the sum of signal and background templates to the data.

The signal discriminant was generated from a simulated $t\bar{t}$ sample which was corrected to match the jet energy resolution observed in the data. An additional flavor-dependent correction was applied to the simulated jets to account for differences in $b$-tag efficiencies between data and simulation. The template shapes for QCD, $W + j$, and $Z + j$ were produced directly from control regions in the data. These were chosen using variables that are only very loosely correlated to the network parameters so that they do not bias the operation of the network.

Because the event topologies of $t\bar{t}$ and single-top events are so similar, there is very little difference in the shapes of the discriminant for the two samples. In order to avoid pathological fit yields due to this similarity, the number of single-top events in the fit was constrained to the expected

### Table V. Correlation matrix of the fit to the combined electron and muon data samples.

<table>
<thead>
<tr>
<th></th>
<th>$t\bar{t}$</th>
<th>$t(\bar{t})$</th>
<th>$W + b$ jets</th>
<th>$W + c$ jets</th>
<th>$W + q\bar{q}$</th>
<th>$Z +$ jets</th>
<th>$Q^2$</th>
<th>$b$ tag</th>
<th>JES</th>
<th>$R_{\text{mistag}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t\bar{t}$</td>
<td>1.0</td>
<td>-0.1</td>
<td>0.1</td>
<td>0.5</td>
<td>0.2</td>
<td>0.0</td>
<td>0.3</td>
<td>-0.7</td>
<td>-0.6</td>
<td>0.0</td>
</tr>
<tr>
<td>$t(\bar{t})$</td>
<td>-0.1</td>
<td>1.0</td>
<td>-0.3</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.1</td>
<td>0.1</td>
<td>0.1</td>
<td>0.0</td>
</tr>
<tr>
<td>$W + b$ jets</td>
<td>0.1</td>
<td>-0.3</td>
<td>1.0</td>
<td>0.4</td>
<td>0.4</td>
<td>0.0</td>
<td>0.6</td>
<td>-0.2</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>$W + c$ jets</td>
<td>0.5</td>
<td>0.0</td>
<td>0.4</td>
<td>1.0</td>
<td>-0.1</td>
<td>0.0</td>
<td>0.6</td>
<td>-0.5</td>
<td>-0.2</td>
<td>0.0</td>
</tr>
<tr>
<td>$W + q\bar{q}$</td>
<td>0.2</td>
<td>0.0</td>
<td>0.4</td>
<td>-0.1</td>
<td>1.0</td>
<td>-0.1</td>
<td>0.5</td>
<td>-0.2</td>
<td>-0.2</td>
<td>-0.3</td>
</tr>
<tr>
<td>$Z +$ jets</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>-0.1</td>
<td>1.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>$Q^2$</td>
<td>0.3</td>
<td>0.1</td>
<td>0.6</td>
<td>0.6</td>
<td>0.5</td>
<td>0.0</td>
<td>1.0</td>
<td>-0.2</td>
<td>0.1</td>
<td>0.0</td>
</tr>
<tr>
<td>$b$ tag</td>
<td>-0.7</td>
<td>-0.1</td>
<td>-0.2</td>
<td>-0.5</td>
<td>-0.2</td>
<td>0.0</td>
<td>-0.2</td>
<td>1.0</td>
<td>0.3</td>
<td>0.0</td>
</tr>
<tr>
<td>JES</td>
<td>-0.6</td>
<td>0.1</td>
<td>0.0</td>
<td>-0.2</td>
<td>-0.2</td>
<td>0.0</td>
<td>0.1</td>
<td>0.3</td>
<td>1.0</td>
<td>0.0</td>
</tr>
<tr>
<td>$R_{\text{mistag}}$</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>-0.3</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>1.0</td>
</tr>
</tbody>
</table>
yield from the NLO single-top cross section with a 30% uncertainty. The QCD and $W/Z + \text{jets}$ likewise share similar shapes in their discriminants. This ambiguity was resolved by constraining the QCD fit yield according to its leading-order cross section, with a 100% uncertainty due to expected differences between the actual QCD cross section and its leading-order calculation. However, as the QCD contribution is small, it has little effect on the final result.

The fit of the neural-network discriminant to events passing selection cuts in the data is shown in Fig. 4. A study using pseudoexperiments with simulated data indicates that the fit introduces a $-3.1\%$ bias in the $t\bar{t}$ yield. This arises due to the use of control regions for the QCD, $W + \text{jets}$, and $Z + \text{jets}$ templates. After correcting for this, we obtain a $t\bar{t}$ event yield of $369 \pm 36(\text{stat})$ events.

The systematic uncertainties are evaluated by shifting the simulation by each systematic uncertainty and reevaluating the result. The resulting pseudoevents are fit with the nominal discriminator templates for $t\bar{t}$ and single-top, and systematically shifted templates for QCD and $W/Z + \text{jets}$. The dominant uncertainty of $+16\%/-18\%$ comes from the $b$-tag efficiencies. When combined with the other contributions, we find a combined systematic uncertainty of $+23\%/_{-18}\%$. After combining this with the $4\%$ uncertainty in the recorded integrated luminosity [8], we obtain a $t\bar{t}$ cross section of $151 \pm 15(\text{stat})^+35_{-28}(\text{syst}) \pm 6(\text{lumi})$ pb.

### B. Muon channel analysis using a muon-in-jet $b$-tagger

We have also performed an analysis in which $b$ jets are identified by the presence of a nonisolated muon. The event selection requires at least three well-reconstructed jets of which at least one contains a muon with $p_T > 4$ GeV and $|\eta| < 2.4$. The backgrounds from events which come from the decay of a $J/\psi$, $Y$, or $Z$ boson, are excluded using selections on the muon pair invariant mass.

The background from $W + b$ jets and $W + c$ jets with a semimuonic decay and $W + l$ light flavor events with a jet that is misidentified as containing a semimuonic decay are estimated from data. We calculate the track taggability from a sample of $\gamma + \text{jet}$ events. This taggability is convoluted with the track distribution in the jets of the pretagged event sample to predict the number of tagged events that should arise from $W + \text{jet}$, $N_{\text{tag, pred}}$. We correct for the fraction of events in this sample that are due to QCD multijets, $F_{\text{QCD}}$, to obtain $N_{W + \text{jet}} = N_{\text{tag, pred}} \cdot (1 - F_{\text{QCD}})$. We estimate $F_{\text{QCD}}$ using the method discussed below. We assign a 30% systematic uncertainty, based on studies of the taggability parametrization as applied to independent control samples, to the tag-rate prediction to account for the simulation uncertainties.

The QCD background was estimated by calculating the fraction of QCD events in the pretag sample. Because of the enrichment in $b\bar{b}$ and $c\bar{c}$ events after requiring the primary muon, a correction factor $k$ is applied to correct for this. The QCD background is then $N_{\text{QCD}} = N_{\text{tag, pred}} \cdot F_{\text{QCD}} \cdot k$. After taking into account the uncertainties in the calculation, we assign a systematic uncertainty in the QCD background of 60%.

The background from Drell-Yan events that survive the $Z$ veto is estimated from simulation. An estimate from data similar to the one described in Ref. [40] was employed to assign a systematic uncertainty to the prediction from simulation. This gives a systematic uncertainty of 17% on the $Z$ mass veto correction. The remaining backgrounds from diboson and single-top production were estimated from simulated samples that were normalized to the theoretical NLO cross sections. Each of these is assigned a 30% systematic uncertainty.

The selection efficiency for signal events prior to the muon-tag requirement is evaluated using simulated $t\bar{t}$ events and the method described previously. The combined systematic uncertainties on the acceptance, due to the simulation uncertainties, is $+6.3\%/-6.1\%$. Because of the relatively soft $p_T$ spectrum of the tag muons, the reconstruction and identification efficiencies were checked using a tag-and-probe analysis [35] of $J/\psi \to \mu^+ \mu^-$ events. The results agree with the simulation to within 1%, so we take the efficiency for finding a tag muon and the mistag efficiency directly from simulation. This gives a tagging efficiency for $t\bar{t}$ events of $25.4 \pm 0.1\%$ excluding the resonance veto requirements, and $23.9 \pm 0.1\%$ including them. The systematic uncertainty on this efficiency is conservatively taken to be 10%. Before calculating the $t\bar{t}$ cross section, the number of predicted tagged events is corrected for the presence of $t\bar{t}$ events in the pretag sample. This correction is performed iteratively. Combining these effects gives a total systematic uncertainty on the $t\bar{t}$ cross section due to the background calculations of 17.9%.

Figure 5 shows the observed jet-multiplicity distribution, together with the signal and background predictions.
Here, the $t\bar{t}$ component is normalized to the NLO cross section [25] and the backgrounds are those computed above. The combined signal and background predictions are in good agreement with the data for each jet-multiplicity.

Combining the data yield, the background estimation, the $t\bar{t}$ acceptance, and the tagging efficiency with all of the associated uncertainties, gives a cross section result of $163 \pm 21^{\text{stat}} \pm 35^{\text{syst}} \pm 7^{\text{lumi}}$ pb. This measurement provides a valuable cross-check of the muon + jets result, as its systematic uncertainties are almost independent of those in the reference analysis.

C. Electron channel cross-check analysis

Our third cross-check analysis is a simple counting analysis using the same displaced vertex tagger as our reference analysis. The event selection requires the presence of at least three well-reconstructed jets, of which one or more is required to be $b$ tagged. We estimate the QCD background from the data using control regions in isolation and the $W + \text{jets}$ background from a combination of data and simulation. To calculate the $t\bar{t}$ event yield, these are subtracted from the data, along with smaller contributions from single-top, Drell-Yan, and diboson production, which are estimated from simulation.

The selection efficiency is calculated for $t\bar{t}$ and for $W + \text{jets}$, and the efficiencies to tag individual jets are measured in bins of jet-$p_T$, separated into $b$, $c$, and $u, d, s, g$ (light) partons. The uncertainties from the data are used in systematic studies as well as the statistical uncertainty from the jet efficiency calculations. The resulting predicted $b$ tag rates applied to simulation of signal and backgrounds are in good agreement with the data (see Fig. 6).

The QCD background estimation is performed using a fit to the electron $I_{\text{rel}}$ distribution in the data above the standard selection where the QCD multijet events dominate. A Gaussian function is used for the central value as it best fits the data, and the fit uncertainty is estimated by varying the $I_{\text{rel}}$ range used in the fit and by using alternate fit functions. The systematic uncertainty from $t\bar{t}$ contamination is evaluated by subtracting the number of $t\bar{t}$ events predicted to be inside the fit region using simulation.

The background due to $W + \text{jets}$ is estimated using a technique motivated by Berends-Giele scaling [41] to measure the jet-multiplicity distribution before $b$-tagging. In strict Berends-Giele scaling, the ratio $C(n)$ of events with $W + \geq n$ jets to events with $W + \geq (n + 1)$ jets is expected to be independent of $n$. To account for an observed deviation from perfect scaling, in this estimate, $C(n)$ is extracted as a linear function of $n$, with slope taken from the simulated event sample for $1 \leq n \leq 3$. The $W + b$ jets content in the simulation is scaled up by a factor of 2, as determined in Sec. IV D.

A $W + \text{jets}$ jet-multiplicity spectrum in data is prepared by applying an additional requirement on the transverse missing energy, $E_T > 20$ GeV, to suppress the QCD background. The number of QCD events remaining in these data are then subtracted by refitting the $I_{\text{rel}}$ distribution as above. The remaining non-$W$ backgrounds and the $t\bar{t}$ content are subtracted from the data sample using Monte Carlo predictions. The normalization of $C(n)$ is then fitted to this data sample. The scale factors obtained are $C(1) = 4.91 \pm 0.13$ and $C(2) = 5.35 \pm 0.16$, where the uncertainties are statistical. Using $C(n)$ the estimate of the $W + \text{jets}$ content in the data with $\geq 3$ jets before $b$ tagging ($N_{W + \text{jets}, \geq 3 \text{jets}}^{\text{pretag, data}}$) is

$$N_{W + \text{jets}, \geq 3 \text{jets}}^{\text{pretag, data}} = \frac{N_{W + \text{jets}, \geq 1 \text{jets}}^{\text{pretag, data}}}{C(1)C(2)}.$$  

(9)
The number of tagged $W + \text{jet}$ events is then found by applying the selection efficiencies described above.

Systematic uncertainties for the $W + \text{jets}$ background estimate are derived by repeating the above process varying $t\bar{t}$ content by 30% as well as varying the normalization of $W + b$ jets by 50% and $W + c$ jets content by factors of 2 and 0.5. Additional fits are also done to Monte Carlo samples where the factorization scale is doubled or halved, as a systematic study. The backgrounds from single-top, Drell-Yan, and diboson production are taken from simulation with a 30% systematic uncertainty.

The background-subtracted and efficiency-corrected yield gives a cross section measurement of $169 \pm 13(\text{stat})^{+39}_{-32}(\text{syst}) \pm 7(\text{lumi})$ pb. The dominant systematic uncertainties are the uncertainties on the $b$-tag scale factors, and the uncertainty on the jet energy scale. This analysis uses a significantly different analysis strategy from the reference electron $+ \text{jets}$ analysis but obtains a very similar cross section. Thus it provides a good cross-check of the method and the results.

### D. Additional cross-check

As a further cross-check, the $t\bar{t}$ cross section was also measured in the muon channel using a simple counting analysis which used the same vertex tagger as our reference analysis. The analysis is similar to that of the electron channel analysis described in the previous subsection. The data were selected using a relaxed $p_T^{\text{rel}}$ cut of $<0.1$ and a missing transverse energy requirement of $\not{E}_T > 20$ GeV. The QCD multijet background was measured from pre-tagged data using the matrix method [42] and the $W + \text{jet}$ background was derived from background-and-signal-subtracted data using the Berends-Giele method described in Sec. V C. After requiring at least three well-reconstructed jets with at least one jet with a $b$ tag and applying a correction of factor of 2 $\pm$ 1 for the $W + \text{heavy flavor}$ content of the simulated data, we find good agreement between the data and simulations. The resulting cross section is in good agreement with our reference result.

### VI. COMBINED CMS MEASUREMENT

In addition to the results from this analysis, CMS has also performed a measurement in the dilepton decay channel [43], where we measured a cross section of dileptons: $\sigma_{t\bar{t}} = 168 \pm 18(\text{stat}) \pm 14(\text{syst}) \pm 7(\text{lumi})$ pb.

To produce a final CMS result, we combine this result with the lepton + jets measurement using a profile likelihood method. This procedure uses the vertex mass templates information from this analysis and adds the dilepton measurements as single bin templates. For the dilepton channels, six statistically independent inputs are used so the uncertainty correlations can be handled correctly. These are the $e\mu$ events with $\geq 2$ jets and no $b$ tag requirement, the $e\mu$, $ee$, and $\mu\mu$ events with only 1 jet, and the $ee$ and $\mu\mu$ events with $\geq 2$ jets and at least 1 $b$ tag. Because different $b$-taggers were used in the two analyses, the $b$-tag uncertainties are treated as uncorrelated. The 3% PDF uncertainty from the lepton + jets measurement is also treated as uncorrelated because it does not relate to anything in the dilepton analysis. The remaining systematic uncertainties (JES, lepton efficiency, renormalization and factorization scales, ME to PS matching, and ISR/FSR) are all assumed to be correlated. The method was verified by using pseudoexperiments, from which it was determined that the likelihood calculation resulted in a 10% underestimate of the errors. We correct for the underestimate in the final result and obtain a combined measurement of

CMS combined: $\sigma_{t\bar{t}} = 154 \pm 17(\text{stat} + \text{syst}) \pm 6(\text{lumi})$ pb.

Figure 7 shows the comparison of the separate and combined CMS [10,43] measurements of the production cross section. The inner error bars on the data points correspond to the statistical uncertainty, while the outer (thinner) error bars correspond to the quadratic sum of the statistical and systematic uncertainties. The outermost brackets correspond to the total uncertainty, including a luminosity uncertainty of 11% (4%) for the 3(36) pb$^{-1}$ results, respectively, which is also added in quadrature.

![Figure 7](color online). Comparison of the CMS measurements for the $t\bar{t}$ production cross sections and the QCD predictions for $\sqrt{s} = 7$ TeV.
Also shown are NLO and approximate NNLO QCD calculations, for comparison. These were computed using the HATHOR program [5] using the calculations from [6]. A common factorization and renormalization scale of $Q = m_t = 173$ GeV was used for the calculations together with the MRTSW 2008 NNLO (NLO) parton distribution functions. The scale uncertainty was determined by independently varying the two scales by factors of 2 and 0.5 and taking the maximum variation as the uncertainty. The PDF uncertainty corresponds to the 90% confidence level (C.L.) uncertainties for the parton distribution functions [29]. This is added in quadrature to the scale uncertainty.

In Fig. 8 we compare these and the $p\bar{p}$ results from the Tevatron [37,38,44,45] to the theoretical predictions as a function of $\sqrt{s}$. These are from the approximate NLO QCD calculations referred to above and the width of the error band corresponds to the variation resulting from changing the $Q^2$ scale up and down by a factor of 2. We find good agreement between the data and the theory in all cases and we note that the combined measurement is already more precise than the NLO QCD prediction.

**VII. SUMMARY OF RESULTS**

We have presented the results of a new analysis of the $t\bar{t}$ production cross section at $\sqrt{s} = 7$ TeV using data recorded by the CMS detector at the LHC during 2010 corresponding to an integrated luminosity of 36 pb$^{-1}$.

Using muon and electron + jets and using $b$-tagging to suppress the backgrounds, we measure cross sections of $\mu +$ jets: $\sigma_{t\bar{t}} = 145 \pm 12$ (stat) $\pm 18$ (syst) $\pm 6$ (lumi) pb, $e +$ jets: $\sigma_{t\bar{t}} = 158 \pm 14$ (stat) $\pm 19$ (syst) $\pm 6$ (lumi) pb from the separate channels. The combination of these gives a cross section of $l +$ jets: $\sigma_{t\bar{t}} = 150 \pm 9$ (stat) $\pm 17$ (syst) $\pm 6$ (lumi) pb.

When combined with the CMS dilepton measurement, we obtain an improved cross section measurement of CMS combined: $\sigma_{t\bar{t}} = 154 \pm 17$ (stat + syst) $\pm 6$ (lumi) pb.

The measurements are in good agreement with the QCD predictions of $164^{+10}_{-13}$ pb [5,6] and $163^{+11}_{-10}$ pb [7] which are based on the full NLO matrix elements and the resummation of the leading and next-to-leading soft logarithms.

**ACKNOWLEDGMENTS**

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